

Example Calculations

Mechanical Analysis

The below data are for a mechanical analysis by the pipette method in which a 40.80 g of air-dry soil were dispersed in 1000 mL of water and two 50 mL aliquots taken. The air-dry moisture content of the soil was 2 % (0.02). What are the percents sand, silt and clay of the sample?

$$\begin{aligned} \text{Mass Dish 1} &= 50.00 \text{ g} \\ \text{Mass Dish 1 + Soil Residue 1} &= 51.20 \text{ g} \end{aligned}$$

$$\begin{aligned} \text{Mass Dish 2} &= 52.00 \text{ g} \\ \text{Mass Dish 2 + Soil Residue 2} &= 52.40 \text{ g} \end{aligned}$$

How to do it

The oven-dry mass equivalent of the air-dry soil was

$$m_{\text{oven-dry}} = 40.80 / (1 + 0.02) = 40.00 \text{ g}$$

The total mass of silt + clay was

$$m_{\text{silt+clay}} = 1.20 \text{ g} \times (1000 \text{ mL} / 50 \text{ mL}) = 24.00 \text{ g}$$

The total mass of clay was

$$m_{\text{clay}} = 0.40 \text{ g} \times (1000 \text{ mL} / 50 \text{ mL}) = 8.00 \text{ g}$$

Therefore,

$$\% \text{ clay} = [8.00 \text{ g} / 40.00 \text{ g}] \times 100 \% = 20 \%$$

$$\% \text{ silt + clay} = [24.00 \text{ g} / 40.00 \text{ g}] \times 100 \% = 60 \%$$

$$\% \text{ silt} = 60 \% - 20 \% = 40 \%$$

$$\% \text{ sand} = 100 \% - 60 \% = 40 \%$$

Particle Density

The below data are for determination of particle density. Calculate the particle density.

Mass of picnometer	20.00 g
Mass of picnometer + air-dry soil	40.80
Gravimetric water content of the air-dry soil	0.04
Mass of picnometer + soil + water (picnometer filled with soil + water)	52.42 g
Mass of picnometer + water (picnometer filled with water)	40.00 g

How to do it

The oven-dry mass equivalent of the air-dry soil was

$$m_{\text{oven-dry}} = 20.80 / (1 + 0.04) = 20.00 \text{ g}$$

The volume of the picnometer filled with water when it also contained soil was

$$V_{\text{water}} = [52.42 \text{ g}_{\text{total}} - 20.00 \text{ g}_{\text{solids}} - 20.00 \text{ g}_{\text{picnometer}}] / 1.00 \text{ g mL}^{-1} = 12.42 \text{ mL}$$

The total volume of the picnometer was

$$V_{\text{total}} = [40.00 \text{ g} - 20.00 \text{ g}] / 1.00 \text{ g mL}^{-1} = 20.00 \text{ mL}$$

Therefore, the volume of soil solids was

$$V_{\text{solids}} = 20.00 \text{ mL} - 12.42 \text{ mL} = 7.58 \text{ mL}$$

Accordingly, the particle density of the soil was

$$\rho_s = 20.00 \text{ g} / 7.58 \text{ mL} = 2.64 \text{ g mL}^{-1} \text{ or } 2.64 \text{ g cm}^{-3}$$

Bulk Density

A 100 cm³ sample of field-moist soil weighed 180 g. After drying at 105 °C for 24 h, it weighed 150 g.

What was the bulk density of the soil?

How to do it

$$\rho_B = 150 \text{ g} / 100 \text{ cm}^3 = 1.50 \text{ g cm}^{-3}$$

What were the gravimetric and volumetric water contents of the field-moist soil?

How to do it

$$GW = [180 \text{ g} - 150\text{g}] / 150 \text{ g} = 0.20$$

$$VW = \{[180 \text{ g} - 150 \text{ g}] / 1.00 \text{ g cm}^{-3}\} / 100 \text{ cm}^3 = 0.30$$

Assuming a particle density of 2.60 g, what was the porosity of the soil? Also, what fraction of the pore space was air-filled?

How to do it

$$\text{Porosity} = 1 - 1.50 \text{ g cm}^{-3} / 2.60 \text{ g cm}^{-3} = 0.42$$

$$\text{Air-filled porosity} = \text{total porosity} - VW = 0.42 - 0.30 = 0.12$$

Thus, the fraction of the total pore space filled with air was $0.12 / 0.42 = 0.29$

Hydraulic Conductivity

You determine the saturated hydraulic conductivity of two soils, X and Y, under the different conditions given below.

	X	Y
Cross sectional area, A	10 cm ²	80 cm ²
Depth of soil, L	10 cm	5 cm
Constant depth of water, D	10 cm	15 cm
Average discharge rate, Q	10 cm ³ h ⁻¹	16 cm ³ h ⁻¹

What are the saturated hydraulic conductivities, K, of soils A and B? Also, if one soil is a silt loam and the other is a clay loam, which is which?

How to do it

From Darcy's Law, $Q = KA\{[D + L] / L\}$,

$$K = Q / (A\{[D + L] / L\})$$

$$K_{\text{soilX}} = 10 \text{ cm}^3 \text{ h}^{-1} / (10 \text{ cm}^2 \{[10 \text{ cm} + 10 \text{ cm}] / 10 \text{ cm}\}) = 0.50 \text{ cm h}^{-1}$$

$$K_{\text{soilY}} = 16 \text{ cm}^3 \text{ h}^{-1} / (80 \text{ cm}^2 \{[15 \text{ cm} + 5 \text{ cm}] / 5 \text{ cm}\}) = 0.05 \text{ cm h}^{-1}$$

Thus, based on conductivities, soil X would be the silt loam and soil Y, the clay loam.

Air- and Water-Filled Pore Space (Degree of Water Saturation)

Continuing with the above, if 133.32 g of air-dry soil X were used, the gravimetric water content of the air-dry soil is 1 %, its particle density is 2.64 g cm⁻³, and the total wet mass of the soil was 177.00 g, what fraction of the pore space was filled with water?

How to do it

There were 177.00 g – [133.32 g / (1 + 0.01)] = 177.00 g – 132.00 g = 45.00 g_{water} (or 45.00 cm³) in the wet soil.

The maximum volume of water that the sample could have contained is the total pore space, i.e., porosity x total volume,

$$(1 - \rho_B / \rho_S) \times V_T = [1 - (132.00 / 264.00)] \times 100.00 \text{ cm}^3 = 50.00 \text{ cm}^3 \text{ water.}$$

So, only 45.00 / 50.00 = 0.90 of the total pore space was filled with water.